The McGraw-Hill Companies

8787 Orion Place Columbus, OH 43240

February 16, 2011

Mr. Jeff Zaring
State Board of Education Administrator
Indiana Department of Education
Room 225 State House
Indianapolis, IN 46204

Dear Mr. Zaring,

McGraw-Hill Education is pleased to have the opportunity to provide comments on the Textbook Advisory Committee reviews, as well as detailed justifications as to why the Indiana State Board of Education should adopt Macmillan/McGraw-Hill *Math Connects* grades 3-5, *Glencoe Algebra 1* and *Glencoe Geometry*.

We fully support Indiana's goal of providing engaging, effective programs that capture the vision of the Common Core State Standards, including the Standards for Mathematical Practice. Our authors, editors, and educational consultants have carefully studied these standards, and we have attempted to address them in our Indiana submissions.

These high-quality programs deliver classroom-tested best practices that ensure students will understand mathematics and demonstrate appropriate mastery. Our curriculum is reflective of cross-disciplinary skills such as critical thinking and problem solving. The responses for each course offer examples of how each program addresses most significant reviewer concerns, as well as the feedback from the Charles A. Dana Center.

We respectfully request that the Indiana State Board of Education reconsider the non-recommended status of Macmillan/McGraw-Hill *Math Connects* grades 3-5, *Glencoe Algebra 1* and *Glencoe Geometry*. Please feel free to contact me if you have any questions or concerns.

Sincerely,

Lisa Carmona

Lisa Carmona

Vice President, PreK-12 Mathematics Editorial

McGraw-Hill School Education Group

PUBLISHER	School Education Group a division of The McGraw-Hill Companies Inc.					
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TITLE	Math Connects, Grade 4					
AUTHOR(S)	Carter, Cuevas, Day, and Mallo	oy				
Edition	1 st	-				
COPYRIGHT	2011					
ISBN	978-0-02-100994-7 and 978-0)-02-1145 <i>€</i>	7-6 (supplement)			

SUMMARY

McGraw-Hill respectfully requests that the Indiana State Board of Education reconsider the non-recommended status of *Math Connects*, Grades 3-5, for the following reasons:

- 1. Overall, *Math Connects*, Grades 3-5 was rated moderate to strong in all categories of Important Mathematical Ideas, Skills and Procedures, and Mathematical Relationships. In addition, the Indiana Textbook Review Committee stated that all standards were well addressed throughout, and rated *Math Connects* a 4, the highest rating.
- 2. McGraw-Hill submitted a crucial supplement along with *Math Connects* to address the Common Core State Standards, which may not have been considered by the committee. The following chart provides additional references to the instructional materials in these supplements to fully address the Common Core State Standards. We have also suggested improvements that would further strengthen our coverage of the Common Core State Standards.
- 3. *Math Connects* received the highest possible rating (4) for each of the mathematical practices from the Indiana Textbook Review Committee. *Math Connects* earned a rating of **strong** for Important Mathematical Ideas for each grade.

Math Connects is a cohesive, comprehensive program that meets the needs of Indiana students and teachers. We believe it should be reconsidered for adoption.

IDENTIFICATION AND JUSTIFICATION

STANDARDS FOR	1 Make some of wall-ward with the same of				
MATHEMATICAL	1. Make sense of problems and persevere in solving them.				
PRACTICE	2. Reason abstractly and quantitatively.				
	3. Construct viable arguments and critique the reasoning of others.				
	4. Model with mathematics.				
	5. Use appropriate tools strategically.				
	6. Attend to precision.				
	7. Look for and make use of structure.				
	8. Look for and express regularity in repeated reasoning.				
RATING	Strong by Indiana Textbook Review Committee, minimal by Charles A. Dana Center				
OUR RESPONSE	The mathematical practices are embedded throughout <i>Math Connects</i> in practical, meaningful ways.				
	A correlation to the mathematical practices can be found on page xvii of the Teacher Edition of Math				
	Connects to the Common Core Standards supplement.				
	 Students are asked to make sense of problems throughout the program, but particularly in 				
	problem-solving skill lessons. Math Connects introduces and applies a four-step problem-				
	solving plan. This method is used to look for entry points to a solution, explain mathematical				
	relationships, and then check answers and verify reasonableness. (see pages 62-63)				
	Students reason abstractly throughout the program. For instance, in Explore lessons, students				
	decontextualize a situation using models, then show their ability to contextualize by applying				
	abstractly to symbols (see pages 196-197).				
	 Students are able to construct viable arguments when they are asked to explain and justify 				
	their solutions. Frequent Talk About It and Writing in Math features provide opportunities for				
	students to listen or read the arguments of others, decide whether they make sense, and ask				
	useful questions to clarify or improve the arguments. The H.O.T. Problems in every lesson				
	present a variety of exercises such as Open Ended, Find the Error, Reasoning, Number Sense,				
	Which One Does Not Belong?, and Writing in Math to address this practice (see page 82).				
	windowing with manifestation is applied in every resson through engaging contexts from				
	everyday life, society, and the workplace. Real-world examples and multiple real-world				
	exercises ask students to make assumptions and approximations to solve problems. In addition,				
	each chapter has a real-world problem-solving situation related to cross-curricular topics (see				

	 Core lessons on estimation, as well as Problem-Solving Investigations using an estimate or exact answer, address using appropriate tools strategically (see pages 58-61 and 62-63). Students routinely consider available tools when solving problems in this feature. Clear definitions within our program along with opportunities to communicate and explain are available (see pages 359-361). Talk About It, Writing in Math, H.O.T. Problems, and Problem-Solving Skill lessons ask students to check their work, state the meaning of the symbols they choose, and give carefully formulated explanations for their work. Students begin to understand the structure of mathematics by learning the properties of numbers. They are introduced to the properties beginning with whole numbers. This forms the basis of understanding the real number system. (see pages 150-153) Previous work with patterns is extended to include repeated reasoning in multiplication and division patterns. (see pages 204-206). Students also begin work with functions by making 			
	tables, identifying patterns, and graphing simple functions on the coordinate plane.			
COMMON CORE STATE STANDARD	4.0A.1 Interpret a multiplication equation as a comparison, e.g., interpret $35 = 5 \times 7$ as a statement that 35 is 5 times as many as 7 and 7 times as many as 5. Represent verbal statements of multiplicative comparisons as multiplication equations.			
RATING	0			
OUR RESPONSE	Standard 4.OA.1 is covered in the <i>Math Connects to the Common Core State Standards</i> , Grade 4 supplement, Lesson 1 Multiply and Compare.			
COMMON CORE STATE STANDARD	4.OA.2 Multiply or divide to solve word problems involving multiplicative comparison, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem, distinguishing multiplicative comparison from additive comparison.			
RATING				
OUR RESPONSE	Standard 4.OA.2 is covered in the <i>Math Connects to the Common Core State Standards</i> , Grade 4 supplement, Lesson 1 Multiply and Compare.			

COMMON CORE STATE STANDARD	4.OA.3 Solve multistep word problems posed with whole numbers and having whole-number are using the four operations, including problems in which remainders must be interpreted. Represer these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding			
RATING	2			
OUR RESPONSE	Standard 4.OA.3 is addressed in Lesson 2-4 on pages 64-67, Lesson 2-5 on pages 72-74, and Lesson 6-4 on pages 246-248. To further address this standard, an additional online lesson will be added.			
COMMON CORE STATE STANDARD	4.OA.4 Find all factor pairs for a whole number in the range 1-100. Recognize that a whole number is a multiple of each of its factors. Determine whether a given whole number in the range 1-100 is a multiple of a given one-digit number. Determine whether a given whole number in the range 1-100 is prime or composite.			
RATING	2			
OUR RESPONSE	Standard 4.OA.4 is addressed in Lesson 4-9 on pages 176-179, Lesson 6-1 on pages 237-239, and Lesson 7-1 on pages 273-275. It is also covered in the <i>Math Connects to the Common Core State Standards</i> , Grade 4 supplement, Lesson 2 Prime and Composite Numbers.			
COMMON CORE STATE STANDARD	4.NBT.1 Recognize that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right. For example, recognize that $700 \div 70 = 10$ by applying concepts of place value and division.			
RATING	1			
OUR RESPONSE	Standard 4.NBT.1 is addressed in Lesson 1-1 on pages 17-19, Lesson 1-2 on pages 22-25, Lesson 6-1 on pages 237-239, and Lesson 8-2 on pages 316-319.			
COMMON CORE STATE STANDARD	4.NF.3a Understand addition and subtraction of fractions of joining and separating parts referring to the same whole.			
RATING	0			
OUR RESPONSE	Standard 4.NF.3a is covered in Lesson IN 9 Add Like Fractions on pages IN34 – IN37 and Lesson IN 10 Subtract Like Fractions on pages IN38 – IN 41. It is also covered in the <i>Math Connects to the Common Core State Standards</i> , Grade 4 supplement, Lesson 3 Add and Subtract Like Fractions.			

COMMON CORE STATE STANDARD	4.NF.3b Decompose a fraction into a sum of fractions with the same denominator in more than one way, recording each decomposition by an equation. Justify decompositions, e.g., by using a visual fraction model. <i>Examples:</i> $3/8 = 1/8 + 1/8 + 1/8$; $3/8 = 1/8 + 2/8$; $21/8 = 1 + 1 + 1/8 = 8/8 + 8/8 + 1/8$	
RATING	1	
OUR RESPONSE	Standard 4.NF.3b is addressed in Lesson 13-6 on pages 560-563. To further address this standard, an additional online lesson will be added.	
COMMON CORE STATE STANDARD 4.NF.3c Add and subtract mixed numbers with like denominators, e.g., by replacing number with an equivalent fraction, and/or by using properties of operations and the between addition and subtraction.		
RATING	0	
OUR RESPONSE Standard 4.NF.3c is covered in the <i>Math Connects to the Common Core State Standard</i> supplement, Lesson 4 Add and Subtract Mixed Numbers.		
COMMON CORE STATE STANDARD	4.NF.3d Solve word problems involving addition and subtraction of fractions referring to the same whole and having like denominators, e.g., by using visual fraction models and equations to represent the problem.	
RATING	0	
OUR RESPONSE	Standard 4.NF.3d is covered in the <i>Math Connects to the Common Core State Standards</i> , Grade 4 supplement, Lesson 3 Add and Subtract Like Fractions.	
COMMON CORE STATE STANDARD	4.NF.4a Understand a fraction a/b as a multiple of $1/b$. For example, use a visual fraction model to represent $5/4$ as the product $5 \times (1/4)$, recording the conclusion by the equation $5/4 = 5 \times (1/4)$.	
RATING	0	
OUR RESPONSE	Standard 4.NF.4a is covered in the <i>Math Connects to the Common Core State Standards</i> , Grade 4 supplement, Lesson 5 Multiply Fractions by Whole Numbers.	
COMMON CORE STATE STANDARD	4.NF.4b Understand a multiple of a/b as multiple of $1/b$, and use this understanding to multiply a fraction by a whole number. For example, use a visual fraction model to express $3 \times (2/5)$ as $6 \times (1/5)$, recognizing this product as $6/5$. (In general, $n \times (a/b) = (n \times a)/b$.)	

RATING	0		
OUR RESPONSE	Standard 4.NF.4b is covered in the <i>Math Connects to the Common Core State Standards</i> , Grade 4 supplement, Lesson 5 Multiply Fractions by Whole Numbers. 4.NF.4c Solve word problems involving multiplication of a fraction by whole number, e.g., by using visual fraction models and equations to represent the problem. For example, if each person at a party will eat 3/8 of a pound of roast beef, and there will be 5 people at the party, how many pounds of roast beef will be needed? Between what two whole numbers does your answer lie?		
COMMON CORE STATE STANDARD			
RATING	0		
OUR RESPONSE	Standard 4.NF.4c is covered in the <i>Math Connects to the Common Core State Standards</i> , Grade 4 supplement, Lesson 5 Multiply Fractions by Whole Numbers.		

COMMON CORE STATE STANDARD	4.NF.5 Express a fraction with denominator 10 as an equivalent fraction with denominator 100, and use this technique to add two fractions with respective denominators 10 and 100. For example,		
	express $3/10$ as $30/100$, and add $3/10 + 4/100 = 34/100$.		
RATING	2		
OUR RESPONSE	Standard 4.NF.5 is addressed in Lesson 14-1 on pages 577-578 and Lesson 14-7 on pages 596-599. To further address this standard, an additional online lesson will be added.		
COMMON CORE STATE STANDARD	4.MD.2 Use the four operations to solve problems distances, intervals of time, liquid volumes, masses of objects, and money, including problems involving simple fractions or decimals and problems that require expressing measurements given in a larger unit in terms of a smaller unit. Represent measurement quantities using diagrams such as number line diagrams that feature a measurement scale.		
RATING	2		
OUR RESPONSE	Standard 4.MD.2 is addressed in Chapter 11 on pages 439-471 and Chapter 12 on pages 485-523. To further address this standard, an additional online lesson will be added.		
COMMON CORE STATE STANDARD	4.MD.4 Make a line plot to display a data set of measurement in fractions of a unit (1/2, 1/4, 1/8). Solve problems involving addition and subtraction of fractions by using information presented in line plots. For example, from a line plot find and interpret the difference in length between the longest and shortest specimens in an insect collection.		
RATING	0		
OUR RESPONSE	Standard 4.MD.4 is covered in the <i>Math Connects to the Common Core State Standards</i> , Grade 4 supplement, Lesson 6 Represent Measurement Data in a Line Plot.		

COMMON CORE STATE STANDARD	4.MD.5a An angle is measured with reference to a circle with its center at the common endpoint of the rays, by considering the fraction of the circular arc between the points where the two rays intersect the circle. An angle that turns through 1/360 of a circle is called "one-degree angle," and can be used
	to measure angles.
RATING	2
OUR RESPONSE	Standard 4.MD.5a is addressed in Lesson 9-4 on pages 368-370 and Lesson IN 5 More Angles on pages IN18 – IN21. In addition, the standard is covered in the <i>Math Connects Common Core State Standards</i> , Grade 4 supplement, Lesson 7 Measure Angles.
COMMON CORE STATE STANDARD	4.MD.5b An angle that turns through <i>n</i> one-degree angles is said to have an angle measure of <i>n</i> degrees.
RATING	0
OUR RESPONSE	Standard 4.MD.5b is covered in the <i>Math Connects to the Common Core State Standards</i> , Grade 4 supplement, Lesson 7 Measure Angles.
COMMON CORE STATE STANDARD	4.MD.6 Measure angles in whole-number degrees using a protractor. Sketch angles of specified measure.
RATING	0
OUR RESPONSE	Standard 4.MD.6 is covered in the <i>Math Connects to the Common Core State Standards</i> , Grade 4 supplement, Lesson 7 Measure Angles and Lesson 8 Draw Angles.
COMMON CORE STATE STANDARD	4.MD.7 Recognize angle measure as additive. When an angle is decomposed into non-overlapping parts, the angle measure of the whole is the sum of the angle measures of the parts. Solve addition and subtraction problems to find unknown angles on a diagram in real world and mathematical problems, e.g., by using an equation with a symbol for the unknown angle measure.
RATING	0
OUR RESPONSE	Standard 4.MD.7 is covered in the <i>Math Connects to the Common Core State Standards</i> , Grade 4 supplement, Lesson 7 Measure Angles.

COMMON CORE STATE STANDARD	i.G. Diaw points, fines, fine segments, rays, angles (fight, acute, obtuse), and bendendicinar and			
RATING	2			
OUR RESPONSE	Standard 4.G.1 is addressed in Lesson 9-4 on pages 368-370 and Lesson 9-5 on pages 372-375. It is also covered in the <i>Math Connects to the Common Core State Standards</i> , Grade 4 supplement, Lesson 8 Draw Angles.			
COMMON CORE STATE STANDARD	4.G.2 Classify two-dimensional figures based on the presence or absence of parallel or perpendicular lines, or the presence or absence of angles of a specified size. Recognize right triangles as a category, and identify right triangles.			
RATING	2			
OUR RESPONSE	Standard 4.G.2 is addressed in Lesson 9-4 on pages 368-370, Lesson 9-5 on pages 372-375, and Lesson 9-6 on pages 376-378. To further address this standard, an additional online lesson will be added.			

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Sincerely,

Lisa Carmona

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Vice President, PreK-12 Mathematics Editorial

McGraw-Hill School Education Group

February 18, 2011

Dear Indiana Educational Reviewer:

In addition to our written comments, we are sending the following documents for your review:

- FedEx tracking information: The items required for review: core program and the new Common Core supplement. Per the memorandum dated September 16, 2010, we are providing proof of delivery for both pieces.
- Math Connects to the Common Core State Standards, Grades 3-5: These documents were part of our original submission (please see tracking information). Reviewers' comments appear to indicate this supplement may have been missed during the initial review.
- •Log-in information to access our teacher materials for the *Math Connects to the Common Core* supplement.

Website: http://glencoe.com/sites/common_assets/ccss/ccss.html

Username: CCSSPassword: Benefits

Thank you.





Math Connects

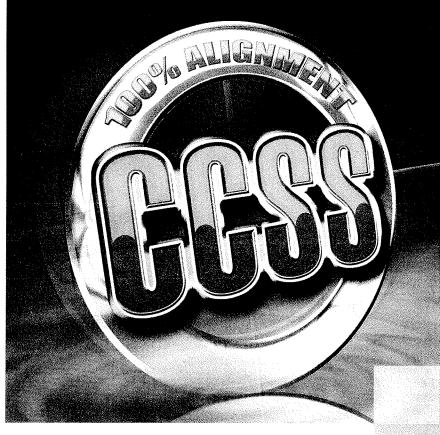




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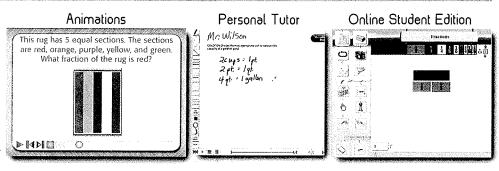
Homework: Lesson 8

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There's more online!

Find these pages in StudentWorks Plus online.



Lesson

Main Idea

I will write whole numbers as fractions.

Vocabulary

fraction

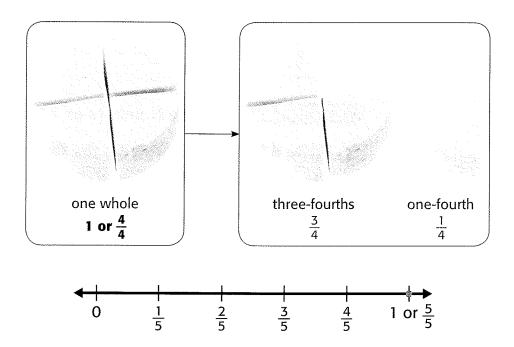
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8888 3.NF.3.c

Fractions as One Whole

Whole numbers can be written as fractions. When the numerator is the same as the denominator, the fraction equals 1.



Key Concept

Fractions as One Whole

$$= 1$$

$$\frac{15}{15} = 1$$

$$\frac{7}{7} = 1$$
 $\frac{15}{15} = 1$ $\frac{329}{329} = 1$

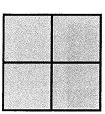
● PIGNITIES One Whole as a Fraction

(1) Write a fraction to describe the figure.

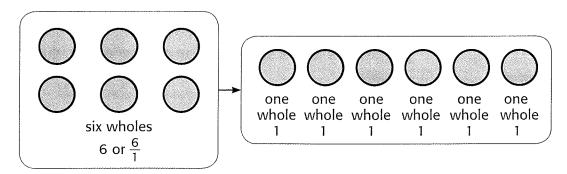
The figure shows one whole. It is divided into four equal parts, or four fourths.

$$\frac{4 \text{ green parts}}{4 \text{ total parts}} = \frac{4}{4}$$

So, the figure shows $\frac{4}{4}$.



When the denominator is 1, the numerator represents the number of wholes.



Whole Numbers as a Fraction ב אַנועוניוני אַ אַ Whole Numbers as a Praction

2) Write a fraction to describe the figures.

The set of figures shows five wholes. Each whole is the same size.







So, the set of figures shows $\frac{5}{1}$.

ತ್ರ) Write 7 as a fraction.

A whole number can be written by writing the number of wholes as the numerator and 1 as the denominator.

$$7 = \frac{7}{1}$$

So, 7 can be written as $\frac{7}{1}$.

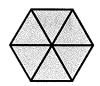
CHECK What You know

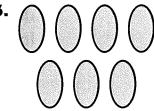
Write a fraction to describe each figure or set of figures.

See Examples 1 and 2



2.





- 4. Write 4 as a fraction. See Example 3
- 5. TALK MATH How can you tell whether $\frac{6}{1}$ is greater or less than 1?
- **Domain:** Number and Operations—Fractions

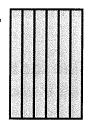
Practice and Problem Solving

Write a fraction to describe each figure or set of figures.

See Examples 1 and 2

6.

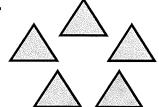


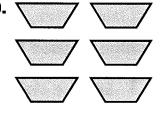


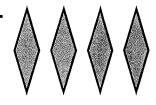
8.



9.







Write each number as a fraction. See Example 3

12. 8

13. 3

14. 5

15. 2

16. 9

17. 4

18. 7

19. 6

Solve.

- **20.** Tim has $\frac{7}{1}$ magazines. He gave 4 of his magazines to Mike. How many magazines does Tim have left? Write this number as a fraction.
- **21.** Leslie has $\frac{6}{1}$ magnets. Jolie has $\frac{3}{1}$ magnets. How many magnets do they have altogether? Write this number as a fraction.

H.O.T. Problems

- 22. OPEN ENDED Draw a picture that represents a whole number. Write a fraction that is greater than what the picture represents and a fraction that is less than what the picture represents.
- **23. WRITE MATH** Write a fraction that is equivalent to 1 whole. Explain how you know it is equivalent.

Lesson 2

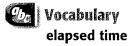
Wain Idea

I will determine the amount of elapsed time to solve problems.

Materials

2 student clocks





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Time Intervals

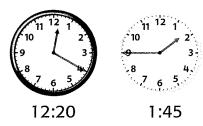
To determine **elapsed time**, find the amount of time that passes from the start of an activity to the end of the activity.

Brooke got in line for the roller coaster at 12:20. It was 1:45 when it was her turn to ride. How much time elapsed while Brooke stood in line?

Explore Mini-Activity

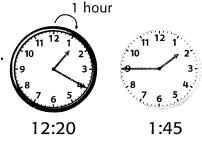
Determine Elapsed Time

Step 1 Set one clock to the start time. Write the time. Set the second clock to the end time. Write the time.



Step 2 Rotate the minute hand of the first clock.

Every time the hand passes the start time, without passing the end time, count 60 minutes or one hour.



Step 3 Continue to rotate the minute hand until the time matches the end time. Count by fives. Then count on by ones, if needed.

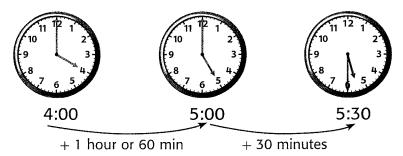
So, Brooke stood in line for 85 minutes or 1 hour and 25 minutes.





TRAVEL It takes Louisa one hour and 30 minutes to travel to her aunt's house. She leaves at 4:00 P.M. What time will she get to her aunt's house?

Add 1 hour and 30 minutes to 4:00 P.M.

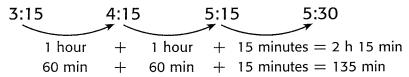


So, Louisa will get to her aunt's house at 5:30 P.M.

2) CHOIR The clock shows the time June's choir practice started. It ended at 5:30 P.M. Find the elapsed time.



Find the elapsed time between 3:15 P.M. and 5:30 P.M.



So, the elapsed time is 2 hours 15 minutes or 135 minutes.

CHECK What You Know

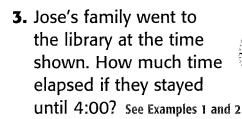
The following are movie times. Find the length of each movie.

See Examples 1 and 2

1. Start Time

End Time





Start time



End time



4. TALK MATH Lupe went to sleep at the time shown at the right and awoke at 6:30 A.M. Explain how to find how long Lupe slept. See Examples 1 and 2

Practice and Problem Solving

The following are times of baseball games. Find the length of each game. See Examples 1 and 2

5. Start Time

End Time





- 6. Start Time
- **End Time**





- **7.** Tyrone went to the mall at 1:10. He left the mall at 4:05. How much time did he spend at the mall?
- **8.** Serena went to the fair at 3:40. She left at 8:35. How much time did Serena spend at the fair?

Find each elapsed time. See Examples 1 and 2

9. The clock shows when Malina began reading her book. It is 12:50 when she stops.



10. The clock shows when Chris went to the park. He stays until 5:15 p.m.



H.O.T. Problems

11. WHICH ONE DOESN'T BELONG? Which set of digital clocks does *not* show an elapsed time of 1 hour 25 minutes? Explain.













- **12. WRITE MATH** Explain how working backward helps you find the amount of time elapsed.
 - 10 Domain: Measurement and Data

Lesson 3

Main Idea

I will solve problems about capacity.

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ccs 3.MD.2, 3.OA.3

Solve Capacity Problems

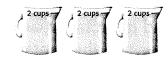
You can solve addition, subtraction, multiplication, and division problems about capacity. Capacity can also be called liquid volume.

Key Concept Capacity Problems				
Addition	2 cups + 2 cups = 4 cups $2 cups + 2 cups = 4 cups$			
Subtraction	4 cups - 1 cup = 3 cups			
Multiplication				
Division				

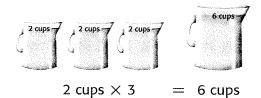
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Customary Capacity Problems

(1) Find the capacity of the total amount of liquid shown in the containers.



There are 3 containers. Each container has 2 cups. So, you need to multiply 2 cups by 3.



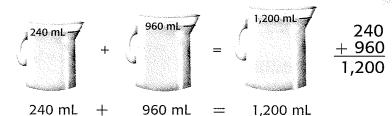
So, there are 6 cups of liquid.

You can also solve problems using metric units of capacity.

Metric Capacity Problems

2) Emily has 240 mL of lemon juice. She needs to add 960 mL of water to make lemonade. How many milliliters of lemonade will she have in all?

You need to add 240 mL and 960 mL.



So, Emily will have 1,200 mL of lemonade.

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Unknown Quantity

Eight containers each have the same amount of juice. There is a total of 24 cups of juice. How much juice is in each container? Write a number sentence to show the unknown quantity, or amount. Then solve.

You can use a symbol to show the unknown amount.

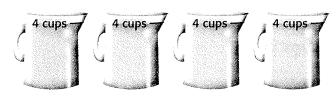
$$8 \times \blacksquare$$
 cups = 24 cups or 24 cups $\div 8 = \blacksquare$ cups You know that $8 \times 3 = 24$ so $24 \div 8 = 3$

So, there are 3 cups of juice in each container.

CHECK What You Know

Write a number sentence to solve. See Examples 1 and 2

1. Find the total capacity of the liquid shown in the containers below.



- 3. Ten cups of juice are divided equally in containers. Each has 5 cups. Write a number sentence to find the unknown number of containers. Then solve.
- 2. Mike has 134 mL of water in a vase. Suppose he adds the water shown below to the 150 mLvase. How much water would be in the vase in all?
- **4. TALK MATH** How did you know which operation to use to solve Exercise 1?

See Example 3

Domain: Measurement and Data

Practice and Problem Solving

Write a number sentence to solve. See Examples 1 and 2

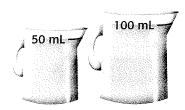
5. Find the total capacity of the liquid shown in the containers below.



7. How much liquid would be left if you poured out 3 cups?



6. Find the total capacity of the liquid shown in the containers below.



8. Suppose you pour this liquid into three containers so that each container has the same amount of liquid. How much liquid would be in each container?

Write a number sentence to show the unknown amount. Then solve. See Example 3

9. George has the cans of soup shown. Each can has the same amount of soup. There are 4 cups of soup in all. How much soup is in each can?



10. Sue has the cans of paint shown. Each can has the same amount of paint. There are 8 gallons of paint altogether. How much paint is in each can?



Algebra Find each missing value.

13.
$$mL \times 4 = 36 \ mL$$

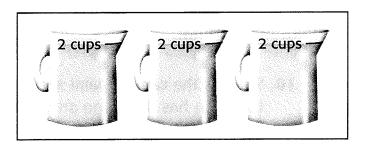
14.
$$132 L - \square L = 43 L$$

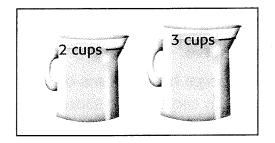
16. Lisa has a vase with 600 mL of water. If she pours out 254 mL of water, how much water will be left in the vase?

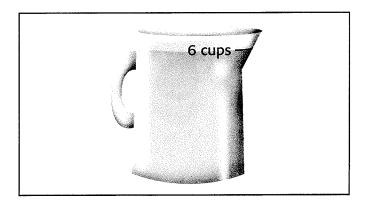
- **17.** Tara has three buckets. Each bucket has 7 liters of water. How many liters of water does she have in all?
- 18. Sean's mother bought a gallon of milk. There are 16 cups in a gallon. If Sean and his brother each have two cups of milk a day, how many days will it take them to drink the entire container of milk?

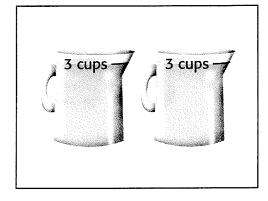
H.O.T. Problems

- 19. CHALLENGE A fish bowl holds 100 mL of water. Suppose the tank is full, and then half of the water is taken out to clean the bowl. Then, 30 mL of water is added back in. Then, half of that water is taken out. How many mL of water need to be added in order to fill the bowl?
- **20. WHICH ONE DOESN'T BELONG?** Which set of containers does not belong? Explain.









- **21. OPEN ENDED** Draw a picture to show a multiplication problem about capacity. Write a story to describe the picture.
- **22. WRITE MATH** Explain why the units need to be the same when solving problems with capacity.
 - 14 Domain: Measurement and Data

Lesson 4

Main Idea

I will solve problems about mass.

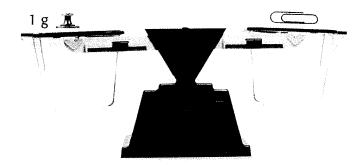
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Solve Mass Problems

You can solve addition, subtraction, multiplication, and division problems about mass. A balance scale can be used to measure mass. On one side you can place the object whose mass you are measuring. On the other side, you can place weights measured in grams. When both sides are equal, you can see that the object has the same mass as the weights.



The balance scale shows that 1 paperclip has a mass of 1 gram.

Solving Mass Problems with a Balance Scale

(1) The balance scale shows the mass of one marker. What is the mass of 5 markers?



Each marker has a mass of 8 grams. So, you need to multiply 8 grams by 5.

8 grams \times 5 = 40 grams

So, five markers have a total mass of 40 grams.

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Solving Mass Problems

2) An apple has a mass of 216 grams. A banana has a mass of 132 grams. What is the total mass of a banana and an apple?



You need to add to find the total mass.

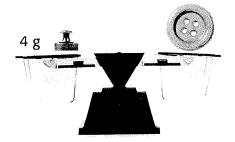
$$\frac{216}{+132}$$

So, an apple and a banana have a total mass of 348 grams.

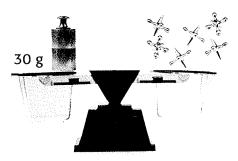


Use the balance scale to solve. See Example 1

1. What is the mass of 9 buttons?



2. What is the mass of one jack?



- **3.** A student has a mass of 34 kilograms. An adult has a mass of 56 kilograms. What is the difference in mass between the student and the adult? See Example 2
- **4. TALK MATH** How did you solve Exercise 2?

16 Domain: Measurement and Data

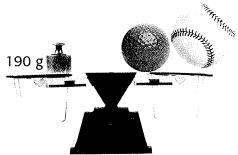
Practice and Problem Solving

Use the balance scale to solve. See Example 1

5. What is the mass of two books?



6. The golf ball has a mass of 45 grams. What is the mass of the baseball?



7. What is the mass of one domino?



Solve. See Example 2

- 8. A toy has a mass of 12 grams. What is the total mass of 6 of these toys?
- **9.** A balance scale shows that two rocks have a total mass of 732 grams. When one of the rocks is removed, the balance scale shows that the remaining rock is 428 grams. What is the mass of the rock that was removed from the scale?

Algebra

10.
$$\blacksquare$$
 g \times 9 = 63 grams

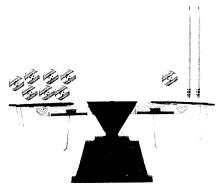
12. 932 g
$$\mathbb{Z}$$
 grams = 149 g

11.
$$392 \text{ kg} + \text{ } \text{ } \text{ } \text{kg} = 523 \text{ kg}$$

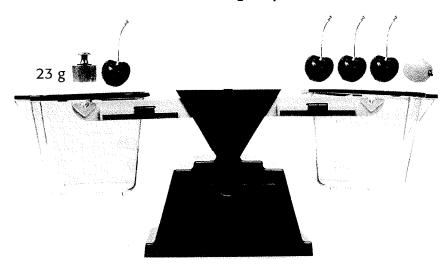
13.
$$60 \text{ kg} \div \mathbb{M} = 5 \text{ kg}$$

H.O.T. Problems

14. CHALLENGE One button has a mass of 3 grams. What is the mass of one pencil?



15. WHICH ONE DOESN'T BELONG? The mass of each cherry shown below is 8 grams. Use the balance scale below to find the sentence that does not belong. Explain.



the mass of 1 cherry = the mass of one grape + 1 gram

the mass of 2 cherries = 16 grams

the mass of 1 cherry = the mass of one grape

the mass of 1 cherry + 4 grams = 12 grams

- **16. WRITE MATH** Write a problem about mass. Have a classmate solve the problem. Check their work.
 - 18 Domain: Measurement and Data

Lesson 5

Main Idea

I will gather measurement data in fractions of an inch and display it in a line plot.

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Gather Measurement Data

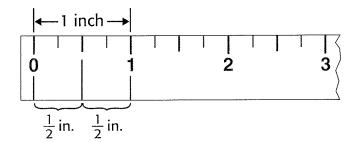
You can gather measurement data by finding the length of several objects. The data collected can be useful.

REAL-WORLD EXAMPLE

Measurement Data

Gather, Organize, and Display Data

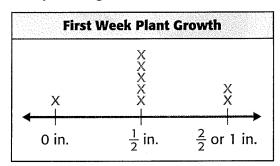
Step 1 Marilyn measured plant growth to the nearest half inch.



Step 2 Marilyn organized the data she collected in a tally chart.

Plant C	irowth
0 in.	1
$\frac{1}{2}$ in.	HH
$\frac{2}{2}$ or 1 in.	11

Step 3 Marilyn made a line plot to show the data she collected. What is the most frequent length the plants grew?

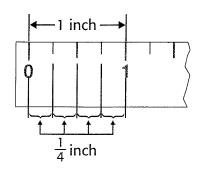


There are more Xs above the half-inch mark on the number line.

So, more plants grew $\frac{1}{2}$ inch the first week.

You can also measure objects to the nearest quarter inch. This allows you to be even more precise with your measurement.

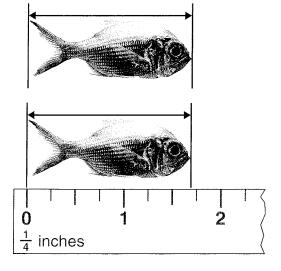
Count the spaces, not the lines. There are four $\frac{1}{4}$ inches in 1 inch.



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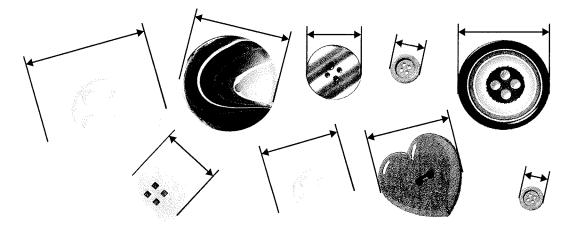
Measurement Data to the Ouarter Inch

- 2) Measure the length to the nearest quarter inch.
 - **Step 1** Estimate the length of the rockfish to the nearest $\frac{1}{4}$ inch.
 - **Step 2** Measure to find the nearest $\frac{1}{4}$ -inch mark at the other end of the fish. How close was your estimate to the actual length? To the nearest $\frac{1}{4}$ inch, this fish is $1\frac{3}{4}$ inches in length.



CHECK What You Know

1. Measure the buttons below to the nearest half inch. Organize the data in a tally chart, and then display it in a line plot. See Example 1

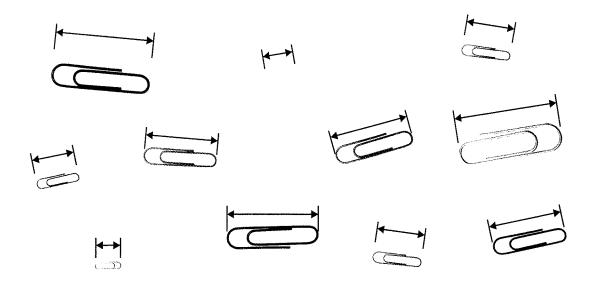


- 2. In what kind of a real-world situation could the data you collected in Exercise 1 be useful?
- **3. TALK MATH** How different would the data be if the measurements taken in Exercise 1 were to the nearest inch, instead of half inch?

20 Domain: Measurement and Data

Practice and Problem Solving

4. Measure the selection of paper clips to the nearest quarter inch. Organize the data in a tally chart, and then display it in a line plot. See Example 1



- **5.** Which length of paper clips are shown the least?
- **6.** What do the numbers on your line plot represent?

For Exercises 7–8, gather the measurement data, organize it in a tally chart, and then display it in a line plot. See Example 1

- **7.** Measure several friends' pencils to the nearest inch. What is the difference in length between the longest and shortest pencil?
- **9.** Write a question about the data you collected in Exercise 7. Ask a classmate to answer it.
- **8.** Measure to the nearest $\frac{1}{4}$ inch, 12 small objects in your classroom that are 2 inches or shorter in length.
- **10.** Write an *answer* for the data you collected in Exercise 8. Ask a classmate to write a *question* for the answer.

H.O.T. Problems

- **11. OPEN ENDED** How are a ruler and the number line of a line plot similar?
- **12. WRITE MATH** Explain how you know which numbers to put on the number line of a line plot.

Lesson 6

Main Idea

I will explore the formula for area.

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Materials

centimeter cubes

9090

centimeter ruler

1	1011	րոր	<u>Imlim</u>	Bulua	ևոսկու	ասիա	mmm
	0	1	2	3	4	5	6
	centimeters						

sticky notes

box

Use a Formula to Find Area

You have found the area of figures by counting the square units. A **formula** can also be used to find area.

Find a formula for area.

Step 1 Make a table.

Copy the table below to record your findings.

Object	Length	Width	Area
sticky note			
box			
book			

Step 2 Measure the length and width of each object.

←length**-≻**

Use the centimeter ruler to measure the length and width of each object.

Step 3 Find the area of each object.

Cover each object with the centimeter cubes. Then count the cubes to find the area.

Step 4 Use a formula to find the area.

Use the data to find how length and width relate to area.

Think About It

- **1.** What operation can you use with the length and width to equal the area?
- 2. What is the formula for the area of a rectangle?
- 22 **Domain:** Measurement and Data

Lesson 7

Main Idea

I will use the area formula to find the area of rectangles.

Vocabulary square units formula

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CCS\$ 3.MD.7.b, 3.MD.7.c

Find the Area of Rectangles

Area is the number of square units needed to cover a region or figure without any overlap. It is measured in **square units**. To find the area, you can count the square units, or you can use a **formula**. The formula for the area of a rectangle is length times width. $A = \ell \times w$

REAL-WORLD EXAMPLE

The Perez family wants to put a sandbox in their backyard. The length is 12 ft. The width is 5 ft. What is the area of the bottom of the sandbox?

One Way: Formula

Multiply the length by the width to find the area.

 $A = length \times width$

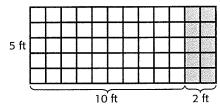
 $A = \ell \times w$

 $A = 12 \text{ ft} \times 5 \text{ ft}$

A = 60 square ft

Another Way: Distributive Property

You can break the rectangle into two parts so that the numbers are easier to multiply. Find the areas of both parts, and then add the parts together.



 $A = 12 \text{ ft} \times 5 \text{ ft}$

 $A = (10 \text{ ft} \times 5 \text{ ft}) + (2 \text{ ft} \times 5 \text{ ft})$

A = (50 square feet) + (10 square feet)

A = 60 square feet

You can also see that there are 60 squares.

So, the area of the sandbox is 60 square feet.

When finding the area of a large object, you may want to use the area formula instead of counting squares.

国主ないバンドラ Area of a Rectangle

PHOTOS Judie is hanging the photo at the right on a wall. How much wall space will the photo need?



7 in.

Use the area formula.

 $A = length \times width$

A = 7 inches \times 5 inches

A = 35 square inches

The photo will need 35 square inches of wall space.

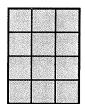
CHECK What You Know

Find the area of each rectangle. See Examples 1 and 2

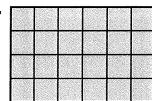
1.



2.



3.



4.

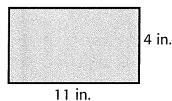


4 m

5.



6.

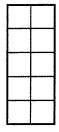


- 7. Mrs. Cole is buying a cover for her swimming pool. The pool's sides are 12 and 9 feet in length. What must be the area of the pool cover?
- 8. TALK MATH How would you find the area of a rectangle that has sides that are 18 and 32 units long? Explain.
- 24 Domain: Measurement and Data

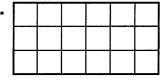
Practice and Problem Solving

Find the area of each rectangle. See Examples 1 and 2

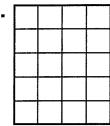
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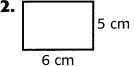
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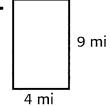
11.



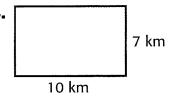
12.



13.



14.



- 15. Ricky's computer monitor is a rectangle. The side lengths are 12 and 8 inches. What is the area of the monitor?
- **16.** A rectangular garden is 4 meters by 6 meters. A bag of soil covers 12 square meters and costs \$7. Find the total cost of covering the garden with soil.
- 17. Steve drew a rectangle that has a length of 7 inches and a width of 3 inches. Sarah drew the rectangle below. Which rectangle has a greater area?

The state of the s		2	in
	8 in.		

18. Tiles cost \$8 per square foot. How much will it cost to tile the table top shown below?

	3	ft
3 ft		

H.O.I. Problems

- 19. OPEN ENDED Draw a rectangle with an area of 24 square units.
- 20. WRITE MATH Explain why two rectangles could each have an area of 12 square units, but have different lengths and widths.

Lesson 8

Main Idea

I will categorize quadrilaterals by the attributes they share.

Vocabulary rhombus parallelogram trapezoid

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Identify Categories of Quadrilaterals

All quadrilaterals have 4 sides and 4 angles.

Some quadrilaterals have two sets of sides that are parallel, or equal distance apart.



These quadrilaterals are called parallelograms.

parallelogram

- opposite sides are the same length and are parallel
- opposite angles are the same



Key Concept

Quadrilaterals

square

- 4 sides of equal length
- opposite sides are parallel
- 4 right angles

rhombus

- 4 sides of equal length
- oppositesides are parallel
- opposite angles are the same

rectangle

- opposite sides of equal length.
- opposite sides are parallel
- 4 right angles

trapezoid

one pair of parallel sides



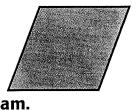
The square, rectangle, and rhombus are quadrilaterals that are also parallelograms.

The trapezoid is a quadrilateral but is *not* a parallelogram. Explain why.

The shared attributes of quadrilaterals help categorize, or group, them into smaller categories.

■ ★★☆☆☆☆☆ Describe and Categorize Shapes

(1) Use the shape's attributes. Categorize the shape in as many ways as possible by describing it as a square, rectangle, rhombus, trapezoid, quadrilateral, or parallelogram.



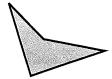
The shape has 4 sides of equal length. Its opposite sides are parallel. Its opposite angles are the same.

So, the shape is a rhombus, quadrilateral, and parallelogram.

■ → (:\\\|:|| = || Draw Quadrilaterals

Draw a quadrilateral that does not belong in any other category.

The shape has four sides. Opposite sides are not equal length or parallel. Its opposite angles are not the same.



This is a quadrilateral and does not belong in any other category.

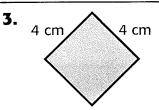
✓ CHECK What You Know

Categorize each shape in as many ways as possible. See Examples 1 and 2

rhombus trapezoid parallelogram quadrilateral rectangle square

1. 10 ft 15 ft

2. 20 in. 10 in. 10 in. 15 in.



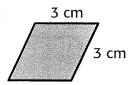
- **4.** Kaila is thinking of a quadrilateral. Its opposite sides are parallel and the same length. There are four right angles. Draw and name the quadrilateral. See Example 1 and 2
- 5. TALK MATH Describe how a square and a rectangle are alike and different.

Practice and Problem Solving

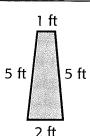
Categorize each shape in as many ways as possible. See Examples 1 and 2

square rectangle rhombus trapezoid parallelogram quadrilateral

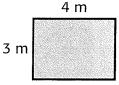
6.



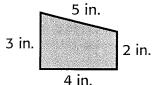
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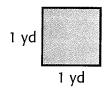
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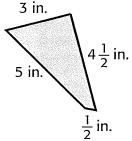
9.



10.



11.



Draw each quadrilateral. See Example 2

- **12.** Draw a quadrilateral that does not belong to any category of quadrilaterals.
- **13.** Draw a shape that is a quadrilateral but is not a parallelogram.

Draw and name each quadrilateral. See Example 2

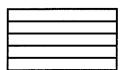
- **14.** This quadrilateral has two pairs of parallel sides of the same length and no right angles.
- **15.** This quadrilateral has opposite sides that are parallel and four right angles. Two sides are longer than the other two sides.

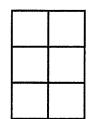
H.O.T. Problems

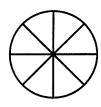
- **16. OPEN ENDED** Draw and identify a quadrilateral that has opposite sides that are the same length and opposite angles that are the same.
- **17. WRITE MATH** Describe how a parallelogram and a square are alike and how they are different.
 - 28 Domain: Measurement and Data

Fractions as One Whole

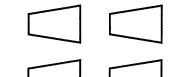
Write a fraction to describe each figure.

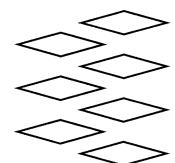


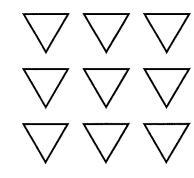




Write a fraction to describe each set of figures.







Solve.

- **7.** Robert had 14 crayons. He used 8 crayons to draw a picture. How many crayons were not used to draw a picture? Write this number as a fraction.
- **8.** Toni has $\frac{33}{1}$ eggs. If she cracks 16 of them, how many will she have left?
- **9.** Draw a picture that represents $\frac{6}{1}$.

2

Homework Practice

Time Intervals

The following are times of activities. Find the length of each activity.

1. Start: 6:15 End: 7:50

2. Start: 4:45 End: 8:00

3. Start: 10:10 End: 12:05

4. Start: 3:30 End: 9:05

Find each elapsed time.

5.



What time will it be in 45 minutes?

6.



What time will it be in 4 hours and 15 minutes?

7.



What time will it be in 9 hours and 10 minutes?

8.



What time will it be in 3 hours and 50 minutes?

Spiral Review

Use any strategy to solve each problem.

9. Pumpkins cost \$2 each. Erika paid the cashier \$10 and received \$6 in change. How many pumpkins did Erika buy?

Solve Capacity Problems

Solve.

- **1.** Find the total capacity of the liquid shown in the containers below.
- **2.** Find the total capacity of the liquid shown in the containers below.

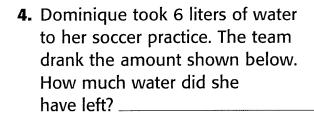








3. Janine is making fizzy fruit punch for her party. She mixes 19 cups of fruit juice with 6 cups of soda. How many cups of punch will she make?







- **5.** Franklin has a cooler that will hold 20 liters of sports drink. How many 2 liter bottles of sports drink will he need to buy to fill the cooler?
- **6.** Trina is helping her dad paint their house. They need 2 gallons of paint for each room. There are 6 rooms in the house. How many gallons of paint do they need?

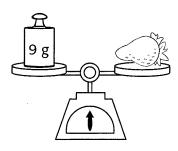
Algebra Find each missing value.

9.
$$mL \times 7 = 56 \ mL$$

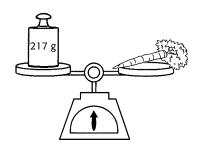
10.
$$129 L - \mathbb{Z} L = 13 L$$

Solve Mass Problems

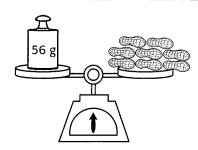
1. What is the mass of 6 strawberries?



2. What is the mass of two carrots?



3. What is the mass of one peanut?



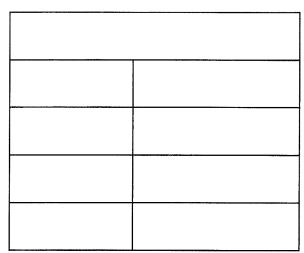
4. A bakery sold a large blueberry muffin that has a mass of 137 grams and a small blueberry muffin that has a mass of 88 grams. What is the difference of mass between the large muffin and the small muffin?

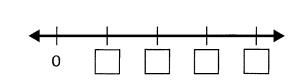
Gather and Display Measurement Data

Represent the following data in a tally chart; then in a line plot.

1. The data represents the length of a handful of broken pretzel sticks in fractions of an inch:

$$\frac{1}{4'}, \frac{2}{4'}, \frac{2}{4'}, \frac{3}{4'}, \frac{1}{4'}, \frac{3}{4'}, \frac{2}{4'}, \frac{3}{4'}, \frac{1}{4'}, \frac{4}{4'}, \frac{1}{4'}, \frac{2}{4}$$





Solve.

2. For which two lengths are there the same number of pretzel sticks? How do you know?

3. Do more or less than half of the pretzel sticks measure half of an inch or shorter? Explain.

4. Write your own question for the data in the line plot above. Then answer it.

Find the Area of Rectangles

Find the area of each rectangle.

Use the grid to draw each of the following rectangles. Then find the area.

3. length: 2 units; width: 6 units



4. length: 3 units; width: 4 units



5. length: 5 units; width: 3 units



6. length: 4 units; width: 6 units



Spiral Review

Find the area of each figure.

7.



8.



9.



10.



11.



12.



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Identify Categories of Quadrilaterals

Check the boxes to categorize each shape in as many ways as possible.

- 1. □ quadrilateral □ parallelogram
 - □ square □ rectangle
 - □ rhombus □ trapezoid

- 2.
 - □ quadrilateral □ parallelogram
 - □ square
 - □ rectangle □ rhombus
 - □ trapezoid

3.



- □ quadrilateral
- □ parallelogram
- □ square
- □ rectangle
- □ rhombus □ trapezoid

Complete the table. Check the attributes that describe each shape every time.

	Four sides	Four right angles	Sides all the same length	Both pairs of opposite sides are equal length	
4. Quadrilateral					
5. Parallelogram					
6. Square					
7. Rectangle					
8. Rhombus					
9. Trapezoid					

Solve.

- **10.** Draw a quadrilateral that is a parallelogram but is not a rectangle.
- 11. Draw a quadrilateral that is not a parallelogram.